





6. Consider the sixth-degree polynomial function $p(x) = -x^6 + 10x^4 - 9x^2$.

(a) Fully factor the polynomial. (3 APP)

$$p(x) = -x^{6} + 10x^{4} - 9x^{2}$$

$$= -x^{2}(x^{4} + 10x^{2} - 9)^{4}$$

$$= -x^{2}(x^{2} - 1)(x^{2} - 9)^{4}$$

$$= -x^{2}(x^{-1})(x^{-1})(x^{-3})(x^{-3})$$

- (c) Use the factored form to solve the equation $-x^6 + 10x^4 9x^2 = 0$. (3 APP)
- $-x^{2}(x-1)(x+1)(x-3)(x+3)=0$ $\therefore x=0 \text{ or } x-1=0 \text{ or } x+1=0$ or x-3=0 or x+3=0 $\therefore x=0,1,-1,3,-3 \sqrt{3}$

b) Use the factored form of the polynomial to sketch the graph of y = p(x). (3 APP)



(d) Use the factored form and the graph to solve the inequality $-x^6 + 10x^4 - 9x^2 \ge 0$. State the solution set using both set notation and interval notation. (4 APP)

 $-x^{2}(x-1)(x+1)(x-3)(x+3) \ge O$ From the graph it's clear that $p(x) \ge 0 \quad \text{if} \quad -3 \le x \le -1, \quad x = 0 \text{ or}$ $1 \le x \le 3. \quad \text{Therefore, the solution}$ set is $\{x \in \mathbb{R} \mid -3 \le x \le -1, \quad x = 0, \quad 1 \le x \le 3\}$ or $E-3, -1] \cup \{0\} \cup [1,3]$

7. Solve the polynomial equation $x^3 - 7x^2 + 16x = 12$. Include a graph that clearly shows the solutions of the equation. (10 TYPS)

 $x^3 - 7x^2 + 16x - 12 = 0$ Let $f(x) = \chi^3 - 7\chi^2 + 16\chi - 12$ Since f(2)=0, x-2 is a factor of f(x) By long division, $f(x)=(x-2)(x^2-5x+6)$ x-5x+6 x-2 x3-7x -16x-12 $(x-2)(x^2-5x+6)=0$ (x-2)(x-2)(x-3)=0 $(x-2)^{2}(x-3)=0$ $(x-2)^2 = 0$, or x-3 = 0TIPS KU APP COM $\therefore x = 2 \text{ or } x = 3$ -0 -0 $-\mathcal{O}$ -0

8. Write an inequality that corresponds to the diagram given at the right. In addition, state the solution set using both set-builder notation and interval notation. (Do not solve the inequility.) You should be able to see the solution just by looking at the graphs.) (5 TIPS) TIPS questions marked halistically
$$y = 3(2x + 4) = 2(x + 4)^{2}$$
.
Trom the graph, it's clear that $5 \le x \le 9$ or $[597]$
Solution Set: $\{x \in \mathbb{R} \mid 5 \le x \le 9\}$ or $[597]$
add degree, possibly 3
9. The polynomial function $f(x) = -x^{n} + kx^{2} - (2k + 2)x + 12$ has two turing points more grants in the values of *n* and *k* as well as any zeros of *f*. Then best approach is to choose the simplest possible value of *n*. (8 TIPS)
Since $f(x)$ can be divided exactly by $x - 3$, $f(0) = 0$
 $\therefore -3^{n} + 8(-3^{n} = 0$
 $\therefore -3^{n} + 9(k - 6(k - 6 + 1) = 0$
 $\therefore -3^{n} + 9(k - 3^{n} = 0$
 $\therefore 3k + 6 - 3^{n} = 0$
 $\therefore 3k - 2 = 0$
 $\therefore 3k - 2 = 0$
 $\therefore 3k - 2 = 0$
 $\therefore 4x = 7$
 $\therefore f(x) = -x^{2} + 9x^{2} - 16x + 12$
 $= -(x - 3)(x^{2} + 2x + 1)$ by long division $= -(x - 3)(x - 2)^{n}$