

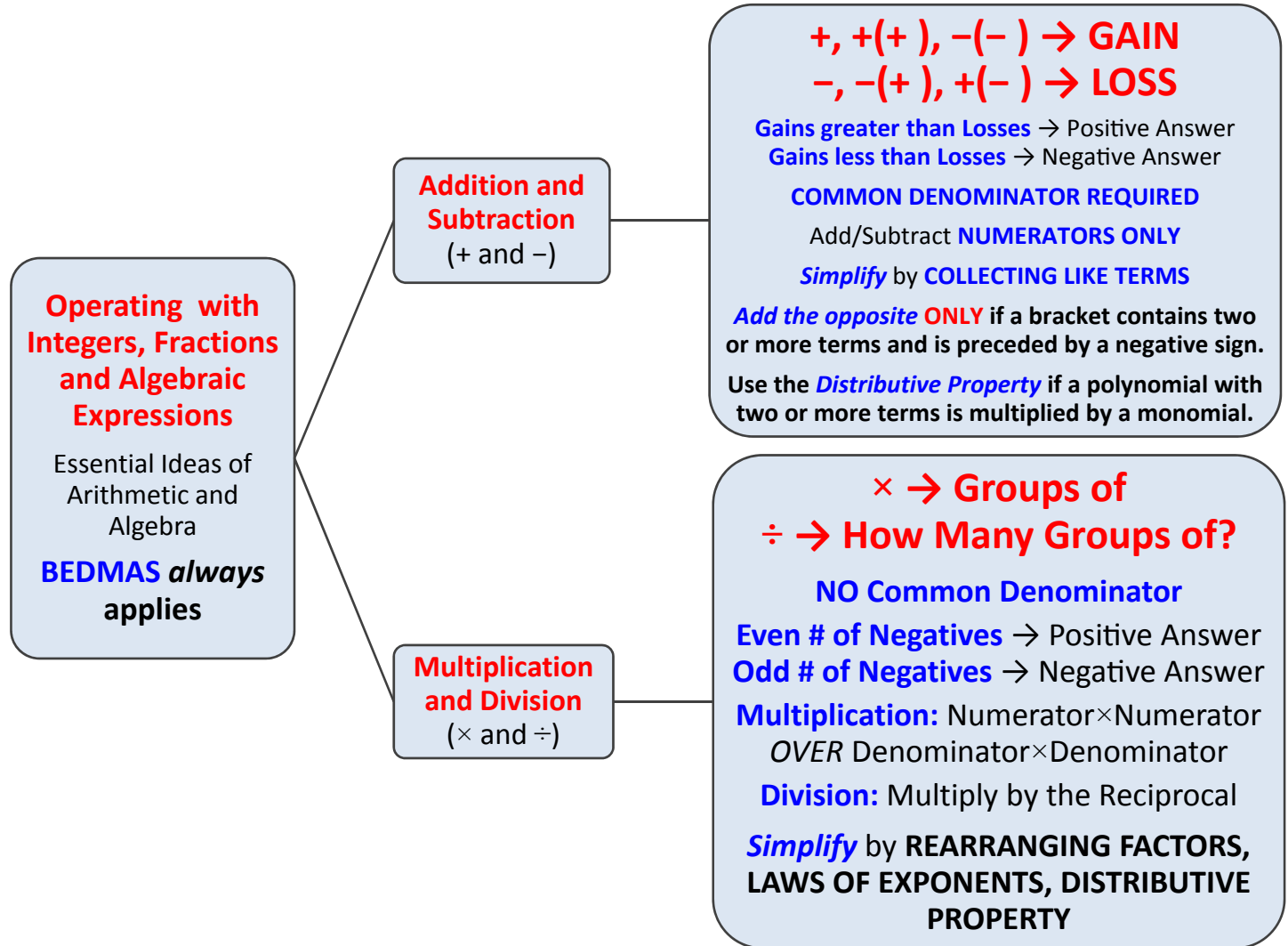
MPM1D0 – UNIT 1 MAKEUP REVIEW

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MAIN IDEAS

Overview of Arithmetic and Mathematical Operations



Summary of Laws of Exponents (Apply ONLY to MULTIPLICATION and DIVISION)

Name of Rule	Algebraic Form	Verbal Form	Example Showing WHY Law Works
Product	$a^x a^y = a^{x+y}$	To multiply two powers with the same base , keep the base and add the exponents .	$a^2 a^4 = (a)(a)(a)(a)(a)(a) = a^6$ Two factors of a multiplied by four factors of a gives six factors of a .
Quotient	$\frac{a^x}{a^y} = a^{x-y}$	To divide two powers with the same base , keep the base and subtract the exponents .	$\frac{a^5}{a^2} = \frac{(a)(a)(a)(a)(a)}{(a)(a)} = a^3$ Five factors of a divided by two factors of a leaves three factors of a .
Power of a Power	$(a^x)^y = a^{xy}$	To raise a power to an exponent, keep the base and multiply the exponents .	$(a^3)^4 = (a^3)(a^3)(a^3)(a^3) = a^{12}$
Power of a Product	$(ab)^x = a^x b^x$	To raise a product to an exponent, raise each factor in the product to the exponent.	$(a^3 b^4 c)^2 = (a^3 b^4 c)(a^3 b^4 c) = a^3 a^3 b^4 b^4 c c = a^6 b^8 c^2$

Examples

1. Evaluate.

LAST!!

$$-5(4^2 - 12^2) - 5(4 - 12)^2$$

BEDMAS

$$= -5(16 - 144) - 5(-8)^2$$

$$= -5(-128) - 5(64)$$

$$= 640 - 320$$

$$= 320$$

LAST!!

Answer is positive because GAIN > LOSS



- **BEDMAS**
- Separate into **terms**.
- Follow **BEDMAS** within each term.
- Be careful with negative values, fractions and powers.

2. Substitute the given values for the variables.

$$-3b^2 - 5a^2b, \text{ if } a = -4 \text{ and } b = -\frac{2}{5}$$

$$= -3\left(-\frac{2}{5}\right)^2 - 5(-4)^2\left(-\frac{2}{5}\right)$$

$$= -\frac{3}{1}\left(\frac{4}{25}\right) - 5(16)\left(-\frac{2}{5}\right)$$

$$= -\frac{12}{25} - \frac{80}{1}\left(-\frac{2}{5}\right)$$

$$= -\frac{12}{25} - \left(-\frac{160}{5}\right)$$

-(-) → GAIN

$$= -\frac{12}{25} + \frac{160 \times 5}{5 \times 5}$$

Common Denominator Required!

$$= -\frac{12}{25} + \frac{800}{25}$$

$$= \frac{-12 + 800}{25}$$

Add NUMERATORS ONLY

$$= \frac{788}{25}$$

Leave answer in improper form



- Replace variables with **empty brackets**.
- Fill in the brackets with given values.
- Follow **BEDMAS** within each term.
- Calculate **carefully** as in the first example.

Rough Work: $\left(-\frac{2}{5}\right)^2 = \left(-\frac{2}{5}\right)\left(-\frac{2}{5}\right) = \frac{2 \times 2}{5 \times 5} = \frac{4}{25}$

answer must be positive

$$5(16) = 80 = \frac{80}{1}$$

$$(-4)^2 = (-4)(-4) = 16$$

answer must be positive

3. Simplify.

$$-7s^3 + 11t^5 - 9s^3 - 12t^5$$

$$= -7s^3 - 9s^3 + 11t^5 - 12t^5$$

Collect Like Terms

$$= -16s^3 - t^5$$

Simplify $-7-9 = -16$
 $+11-12 = -1$

Note: $t^5 = 1t^5$

REMEMBER! 2 cows + 4 cows = 6 cows
2 boys + 4 boys = 6 boys

BUT 2 cows + 4 boys $\neq$ 6 cowboys



- **Addition & Subtraction**
- Collect Like Terms
- Gains/Losses
- To avoid careless arithmetic errors, use a calculator to check answers.

4. Simplify.

No operation between brackets
• understood to be **MULTIPLICATION!**

$$\begin{aligned} & (-7s^3)(+11t^5)(-9s^3)(-2t^5) \\ &= (-7)(+11)(-9)(-2)s^3s^3t^5t^5 \\ &= -1386s^6t^{10} \end{aligned}$$

Since $\times$ can be performed in any order
factors can be rearranged in any order

$s^3s^3 = s^{3+3} = s^6$
 $t^5t^5 = t^{5+5} = t^{10}$

Like terms should **NOT** enter your mind because there is no add/subtract



- **MULTIPLICATION!**
- Although the expression resembles the one in example 3, it is **very different!**
- Simplify by **rearranging factors** and using **laws of exponents**.

5. Simplify.

$$\begin{aligned} & \frac{-52x^{10}y^7}{13x^3y^6} \\ &= \left(\frac{-52}{13}\right)\left(\frac{x^{10}}{x^3}\right)\left(\frac{y^7}{y^6}\right) \\ &= -4x^7y \end{aligned}$$

- Rewrite as a product of "fractions."
- Simplify each "fraction."

Like terms should **NOT** enter your mind because there is no add/subtract



- **MULTIPLICATION AND DIVISION!**
- Rewrite as a product of "fractions."
- To divide two powers with the same base, **keep** the base and **subtract** the exponents.

Rough Work:

$$\frac{-52}{13} = -52 \div 13 = -4, \quad \frac{x^{10}}{x^3} = x^{10-3} = x^7, \quad \frac{y^7}{y^6} = y^{7-6} = y^1 = y$$

6. Simplify

$$\begin{aligned} & (-7s^2 - 11s) - (9s^2 + 2s) \\ &= -7s^2 - 11s + (-9s^2 - 2s) \\ &= -7s^2 - 11s + (-9s^2) - 2s \\ &= -7s^2 - 11s - 9s^2 - 2s \\ &= -7s^2 - 9s^2 - 11s - 2s \\ &= -16s^2 - 13s \end{aligned}$$

add opposite



- **Add the opposite only** when a bracket is preceded by a "-" sign!
- Brackets can be removed if preceded by a "+"
- Collect Like Terms
- Gains/Losses

7. Simplify.

$$\begin{aligned} & -3(2d^2 - 8d) - 3d(d^2 - 8d) \\ &= -6d^2 + 24d - 3d^3 + 24d^2 \\ &= -6d^2 + 24d^2 + 24d - 3d^3 \\ &= 18d^2 + 24d - 3d^3 \end{aligned}$$



- **Distributive Property!**
- Do **not** add the opposite! This will only complicate matters!
- After multiplying, collect like terms.

PRACTICE!

Day 1

1. Evaluate.

(a) $-3[6^2 - 12(-5)^2] - 5[14 + 2(-12)]^2$	(b) $-7a^2b - 2ab^2$, if $a = -\frac{2}{7}$ and $b = -13$
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2. Simplify.

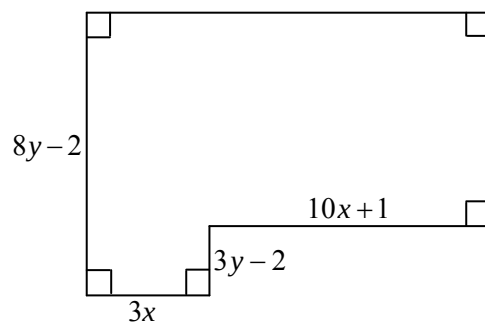
(a) $-17s^3t^4 - 11s^4t^3 + 9s^3t^4 - (-6s^4t^3)$	(b) $(-17s^3t^4)(-11s^4t^3)(-9s^3t^4)(-6s^4t^3)$	(c) $\frac{-108x^{15}y^{17}}{-12x^{14}y^{13}}$
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3. Simplify.

(a) $(-8s^2 - 13s) - (11s^2 + 12s)$	(b) $\frac{100b^9d^2(-bd^3)}{2(5b^4d)^2}$	(c) $-3d(2d^2 - 8d) - 3d^2(d^2 - 8d)$
--	--	--

4. Write **fully simplified** algebraic expressions for...

(a) ...the **perimeter** of the figure at the right.



(b) ...the **area** of the figure at the right.

5. The *KatContrarian Loudspeaker Company* is producing a new ultra-loud speaker for P.A. systems. Each speaker costs \$50.00 to make but there is also a \$3000 set-up charge for the machinery used to make them.

(a) Write an algebraic expression that represents the **total cost** of **manufacturing** n speakers. (n represents the number of speakers manufactured)



(b) *KatContrarian Loudspeaker* sells each speaker for \$200.00. Write an algebraic expression that represents the **total amount of money obtained** for **selling** n speakers. (n represents the number of speakers sold)

(c) How many speakers does *KatContrarian Loudspeaker* need to sell to make a **profit**?

Day 2

1. Evaluate.

(a) $-5[7^2 + 3(-2)^5] - 5[1 + 2(-1)]^5$	(b) $-5a^3b - 4ab^3$, if $a = -\frac{2}{3}$ and $b = -3$
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2. Simplify.

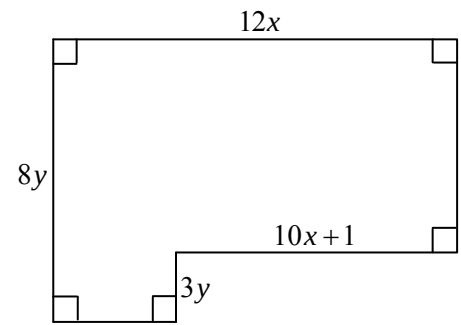
(a) $11xy - 8xy^2 + (-11xy) - 3xy^2$	(b) $(11xy)(-8xy^2)(-11xy)(-3xy^2)$	(c) $\frac{-108a^5b^7}{-24a^4b^7}$
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3. Simplify.

(a) $-(-8s^2 - 13s) + (11s^2 - 12s)$	(b) $\frac{48b^9d^7(-2b^7d^3)}{2(4b^4d^3)^2}$	(c) $-3d(-2d^2 + 8d) - 3d^2(-d^2 + 8d)$
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4. Write **fully simplified** algebraic expressions for...

(a) ...the **perimeter** of the figure at the right.



(b) ...the **area** of the figure at the right.

5. The AvJo toy company is planning to produce a new toy truck. Each one costs \$3.00 to make and there is a \$300 set-up charge for the machinery to make them.

(a) Write an expression that represents the **total cost** of **manufacturing** n trucks.

(b) AvJo sells each truck for \$5.00. Write an expression that represents the **total money obtained** for **selling** n trucks.

(c) How many trucks does AvJo need to sell to make a profit?



Day 3

1. Evaluate.

(a) $-2\left[\left(-\frac{1}{4}\right)^2 - 12(-1)^2\right] - 5[24 + 2(-12)]^2$	(b) $-a^2b^2 - 3a^3b^2$, if $a = -\frac{1}{3}$ and $b = -1$
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2. Simplify.

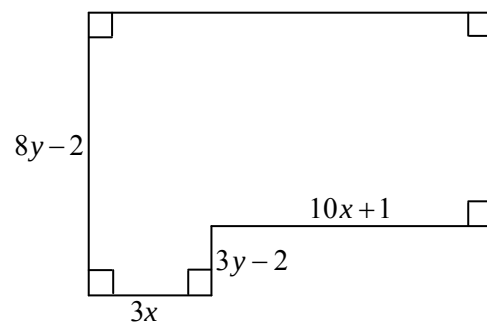
(a) $-17s^3t^4 - 11s^4t^3 + 9s^3t^4 - (-6s^4t^3)$	(b) $(-17s^3t^4)(-11s^4t^3)(-9s^3t^4)(-6s^4t^3)$	(c) $\frac{-108x^{15}y^{17}}{-12x^{14}y^{13}}$
--	---	---

3. Simplify.

(a) $(8ab^2 - 21a^2b) - (-8ab^2 + 21a^2b)$	(b) $\frac{-100u^9v^2(-u^3v)}{2(5u^4v)^3}$	(c) $-3m(2m^2 - 5n) - 3m^2(m - n)$
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4. Write *fully simplified* algebraic expressions for...

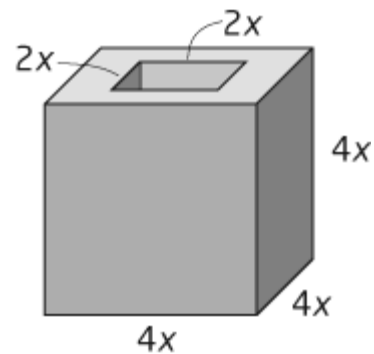
(a) ...the *perimeter* of the figure at the right.



(b) ...the *area* of the figure at the right.

5. A square hole is cut all the way through a cube.

(a) Find the volume of the shape that remains.



(b) Find the surface area of the shape.

Day 4

1. Evaluate.

(a) $-3[4 - 2(-5)]^2 - 5[4^3 + 5(-2)^3]$	(b) $-7a^2b - 2ab^2$, if $a = -3$ and $b = -\frac{5}{6}$
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2. Simplify.

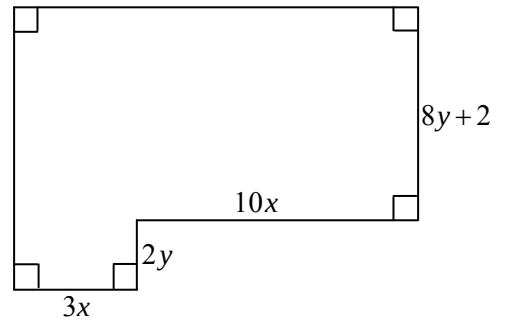
(a) $-17cd - 11d + 9cd - (-6d)$	(b) $(-17cd)(-11d)(-9cd)(-6d)$	(c) $\frac{108m^{15}n^{17}}{-72m^{10}n^{16}}$
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3. Simplify.

(a) $(-8s - 13s^2) - (12s^2 - 11s)$	(b) $\frac{100b^9d^2(-5b^4d^8)}{2(5b^4d)^3}$	(c) $-3d(8d - 2d^2) - 3d^2(8d - d^2)$
--	---	--

4. Write **fully simplified** algebraic expressions for...

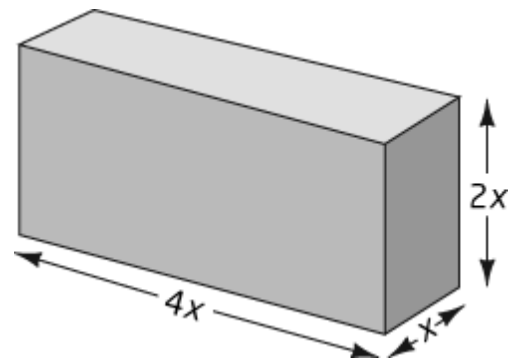
(a) ...the **perimeter** of the figure at the right.



(b) ...the **area** of the figure at the right.

5. Consider the rectangular prism shown at the right.

(a) Write a fully simplified algebraic expression that represents the **volume** of the prism.



(b) Write a fully simplified algebraic expression that represents the **surface area** of the prism.

(c) What is the **edge length** of the **cube** that has the **same volume** as this rectangular prism? Explain your reasoning.

Answers

Day 1	Day 2	Day 3
1. (a) 292 (b) 104 2. (a) $-8s^3t^4 - 5s^4t^3$ (b) $10098s^{14}t^{14}$ (c) $9xy^4$ 3. (a) $-19s^2 - 25s$ (b) $-2b^2d^3$ (c) $18d^3 + 24d^2 - 3d^4$ 4. (a) $P = 26x + 16y - 2$ (b) $A = 74xy - 6x + 5y$ 5. (a) $50n + 3000$ (b) $200n$ (c) The profit is given by the expression $150n - 3000$. This expression must have a positive value for the company to make a profit. If n is 21 or higher, the expression yields a positive value.	1. (a) 240 (b) $-\frac{688}{9}$ 2. (a) $-11xy^2$ (b) $-2904x^4y^6$ (c) $\frac{9}{2}a$ or $\frac{9a}{2}$ 3. (a) $19s^2 + s$ (b) $-3b^8d^4$ (c) $-18d^3 - 24d^2 + 3d^4$ 4. (a) $P = 24x + 16y$ (b) $A = 66xy - 3y$ 5. (a) $3n + 300$ (b) $5n$ (c) The profit is given by the expression $2n - 300$. This expression must have a positive value for the company to make a profit. If n is 151 or higher, the expression yields a positive value.	1. (a) $\frac{191}{8}$ (b) 0 2. (a) $-8s^3t^4 - 5s^4t^3$ (b) $10098s^{14}t^{14}$ (c) $9xy^4$ 3. (a) $16ab^2 - 42a^2b$ (b) $\frac{2}{5}$ (c) $-9m^3 + 15mn + 3m^2n$ 4. (a) $P = 26x + 16y - 2$ (b) $A = 74xy - 6x + 5y$ 5. (a) $V = (4x)^3 - (4x)(2x)^2$ $= 4^3x^3 - (4x)(2^2x^2)$ $= 64x^3 - (4x)(4x^2)$ $= 64x^3 - 16x^3$ $= 48x^3$ (b) $A = 6(4x)^2 + 4(4x)(2x) - 2(2x)^2$ $= 6(16x^2) + 32x^2 - 2(4x^2)$ $= 96x^2 + 32x^2 - 8x^2$ $= 120x^2$
Day 4		
1. (a) -708 (b) $\frac{170}{3}$ 2. (a) $-8cd - 5d$ (b) $10098c^2d^4$ (c) $-\frac{3}{2}m^5n$ or $-\frac{3m^5n}{2}$ 3. (a) $3s - 25s^2$ (b) $-2bd^7$ (c) $-18d^3 - 24d^2 + 3d^4$	4. (a) $P = 26x + 20y + 4$ (b) $A = 110xy + 26x$ 5. (a) $V = x(2x)(4x) = 8x^3$ (b) $A = 2(x)(2x) + 2(2x)(4x) + 2(x)(4x)$ $= 4x^2 + 16x^2 + 8x^2$ $= 28x^2$ (c) $2x$ because $(2x)(2x)(2x) = (2x)^3 = 8x^3$	