MPM1D Exam Review – Unit 1

(Focus on Integers and Rationals)

- **1.** Add or subtract. Express your answers in lowest terms.
 - **a**) $\frac{7}{8} + \frac{5}{8}$ **b**) $\frac{5}{6} - \frac{1}{3}$ **c**) $\frac{2}{3} + \frac{1}{5}$ **d**) $2\frac{1}{4} - \frac{5}{6}$
- **2.** Multiply or divide. Express your answers in lowest terms.
 - **a**) $\frac{4}{15} \times \frac{5}{8}$ **b**) $\frac{1}{3} \div \frac{5}{9}$ **c**) $3\frac{2}{7} \times 4\frac{2}{3}$ **d**) $1\frac{1}{5} \div \frac{5}{6}$
- 3. Donald needs \$20 to buy a ticket to a show. He earned $\frac{1}{4}$ of the money on Monday, $\frac{2}{5}$ on Tuesday, and $\frac{1}{10}$ on Wednesday. What fraction of the money does Donald still need to earn?
- **4.** Find each sum, difference, product, or quotient.

a)	-8 + 3	b)	6 + (-8)
c)	-2 + (-5)	d)	7 – (–3)
e)	-12-9	f)	-1 - (-4)
g)	-25×3	h)	$11 \times (-4)$
i)	$-50 \times (-4)$	j)	72 ÷ (-8)
k)	$-60 \div (-12)$	D	$-24 \div 4$

- 5. Evaluate.
 - a) $32 \div (-4) \times 3$
 - **b**) $(-2) \times 6 + (-4)$
 - **c**) $-64 \div 8 \div (-2)$
 - **d**) 23 + (-7) (-5) 6
- 6. Kate borrowed \$7 from her parents on each of the last 4 days. This morning she paid her parents \$20. How much does Kate still owe her parents?

- 7. Evaluate.
 - a) $-16 + 4 \times (-3)$ b) $35 \div (-7) + (-3)(-5)$ c) $(6 - 18) \times (-8 + 2)$ d) $5(14 - 11)^2 - (-2)$ e) $10 + 8 - 12 \div (-4)$
 - e) $-10 + 8 12 \div (-4) \times 2$ f) $-30 \div 5 \times 2 + (-8)$
 - **g**) $[(6^2 + 3) \div 13]^2$
 - **h**) $(12 + 9) \div (-20 + 17)$
- 8. Martine deposited \$15 in her bank account each week for 6 weeks. Then she withdrew \$8 each week for 9 weeks. How much money does Martine have left in her bank account?
- **9.** Evaluate each of the following:

a)
$$\frac{-2}{5} + \frac{12}{5}$$

b) $\frac{-2}{3} - \frac{5}{9}$
c) $3\frac{1}{4} - 5\frac{5}{6}$
d) $\left(\frac{3}{-4}\right)\left(\frac{-8}{9}\right)$
e) $2\frac{4}{5} \div \left(-3\frac{1}{3}\right)$
f) $\left(\frac{12}{-5}\right)\left(\frac{15}{-8}\right)\left(\frac{-4}{21}\right)$

Answers				
1.	a) $\frac{3}{2}$	b) $\frac{1}{2}$	c) $\frac{13}{15}$	d) $1\frac{5}{12}$
2.	a) $\frac{1}{6}$	b) $\frac{3}{5}$	c) $15\frac{1}{3}$	d) $1\frac{11}{25}$
3.	$\frac{1}{4}$			
4.	a) -5	b) -2	c) -7	d) 10
	e) -21	f) 3	g) -75	h) -44
	i) 200	j) –9	k) 5	l) -6
5.	a) –24	b) -16	c) 4	d) 15
6.	\$8			
7.	a) –28	b) 10	c) 72	d) 47
	e) 4	f) -20	g) 9	h) –7
8.	\$18			
9.	a) 2	b) $\frac{-11}{9}$	c) $\frac{-31}{12}$	d) $\frac{2}{3}$
	e) $\frac{-21}{25}$	f) $\frac{-6}{7}$		

- **1.** Evaluate.
 - **a)** 5^3 **b)** 2^8 **c)** -3^4 **d)** $(-2)^4$ **e)** $(-1)^{10}$ **f)** $\left(\frac{2}{3}\right)^3$
- **2.** Evaluate. Use the correct order of operations.
 - **a)** $3^4 + 4^2$ **b)** $7^2 - 7$ **c)** $9^2 \div 3^2$ **d)** $5 \times \left(\frac{2}{5}\right)^3$ **e)** $(3^2 + 4^2)$ **f)** $(3 + 4)^2$
- **3.** Write as a single power. Then, evaluate.
 - a) $8^5 \times 8^4 \div 8^7$ b) $6^7 \div 6^5 \div 6$ c) $(3^3)^4 \div 3^9$ d) $\frac{(5^3)^4 \times 5^2}{5^{10}}$ e) $2^7 \times 2^5 \div (2^2)^4$ f) $[(-6)^3]^3 \div [(-6)^2]^4$
- 4. Simplify.

a)
$$b^{6} \times b^{3}$$

b) $g^{2} \times g^{8} \div g^{7}$
c) $(a^{5})^{3} \div (a^{4})^{2}$
d) $m^{5}n \times m^{2}n^{4}$
e) $p^{7}q^{4} \div p^{3}q^{4}$
f) $\frac{8b^{3}d \times 4bd^{2}}{2(2bd)^{2}}$

- **5.** Identify the coefficient and the variable for each term.
 - **a)** 7m **b)** $-3x^5$ **c)** $\frac{3}{7}m^2n$ **d)** gh
- **6.** Classify each expression as a monomial, binomial, trinomial, or polynomial.
 - a) $a^2 2a + 1$ b) $2 - 3x^4 - 5x^2 + 4x$ c) $6m^2n^5$

- 7. State the degree of each term.
 - **a)** $-8b^4$ **b)** $-x^4v^3$
- 8. Simplify each expression.
 - a) 2b + 7g 5b 8gb) $3x + y^2 + 5y^2 - 7x$ c) 6q + u + 4u + q + u + 4u - ud) $10 - m^2 - 7 - m^2 + 4m^2$ e) -3v + 2v + 6 - 3v - 9 - v
 - **f**) 7 + h + h 5 + 6h + 2 + 3h
- 9. Simplify.
 - a) (6k-4) + (2k+4)b) (2a+1) - (4a+2)c) (b-6) - (2-5b) + (b+4)d) (g+12) + (g-7) - (2-3g)e) $(x^2 + 2x + 1) + (2x^2 + 4)$ f) $(2m^2 + m + 12) - (3m^2 + 4m - 6)$
- 10. Expand.
 - a) 5(x+3)b) 4(b+2)c) w(2w+1)d) q(q+4)e) 3c(6-4c)f) -p(2p-1)g) $-5(a^2-4a-2)$ h) $2d(d^2-3d-1)$
- **11.** Expand and simplify.
 - a) 3(x + 3) + 2(x + 1)b) -4(m + 2) + 3(m - 7)c) -(d - 3) - 5(d + 2)d) 5[b + 2(b + 1)]e) -2[3(a + 3) - 4]
 - **f**) 4[-2(4-t)+3t]

Unit 2 Answers **1. a**) 125 **b**) 256 **c**) -81 **f**) **d**) 16 e) 1 **2. a**) 97 b) 42 **c**) 9 **d**) $\left(\frac{8}{25}\right)$ **e**) 25 **f**) 49 **a)** 8^2 ; 64 **b**) 6^1 ; 6 **c**) 3^3 ; 27 3. **d**) 5⁴; 625 **e**) 2^4 ; 16 **f**) $(-6)^1$; -6 **a**) b^9 **b**) g^3 4. c) a^{\prime} **d**) $m^7 n^5$ **e**) p^4 **f**) $4b^2d$ a) coefficient: 7; variable *m* 5. **b**) coefficient: -3; variable x^5 c) coefficient: $\frac{3}{7}$; variable $m^2 n$ **d**) coefficient: 1; variable *gh* 6. a) trinomial **b**) polynomial c) monomial 7. **a**) 4 **b**) 7 **b**) $-4x + 6y^2$ 8. **a**) -3b - g**c**) 7q + 9u**d**) $3 + 2m^2$ e) -5v - 3**f**) 4 + 11*h* 9. **b**) -2*a* - 1 **a**) 8k **c**) 7b - 4**d**) 5*g* + 3 e) $3x^2 + 2x + 5$ **f**) $-m^2 - 3m + 18$ **10. a**) 5*x* + 15 **b**) 4*b* + 8 c) $2w^2 + w$ **d**) $q^2 + 4q$ e) $18c - 12c^2$ **f**) $-2p^2 + p$ **g**) $-5a^2 + 20a + 10$ **h**) $2d^3 - 6d^2 - 2d$ **b**) -*m* - 29 **11.** a) 5x + 11c) -6d - 7**d**) 15*b* + 10 **e**) -6a - 10**f**) -32 + 20t

<u>Unit 3 Review (Equations and Problem</u> <u>Solving)</u>

1. Solve.

a)	5y = 35	b)	b - 8 = -12
c)	$\frac{x}{4} = 7$	d)	h + 5 = 13

- 2. Solve.
 - **a**) 8m + 9 = -15
 - **b**) 2p + 7 = 3
 - c) 5 4k = -7
 - **d**) 4 + 3c = -12
- **3.** Solve, then check with a formal verification.
 - **a**) -2a = -22
 - **b**) 3 q = -5

- **c**) $\frac{1}{2}g = -9$ **d**) 7 - 6s = 19
- 4. Solve.
 - a) 2m + 5m 3 = 4b) 4b - 6 + b - 9 = 0c) 3x - x + 4 = 0d) 2k + 3 = 4k - 5
- 5. Solve.
 - a) 2 + (4h 1) = 11 + 2hb) 8 - (2g + 3) = 3g - 5c) 2(d + 6) = 9(d - 1)
 - **d**) 5(3r-7) + r = 3(r-3)
- 6. Solve.
 - **a**) 4s + 3 s = -6
 - **b**) p 3 + 2p 9 = 0
 - c) 5 (c+3) = 4 + c
 - **d**) 3(4d-7) 6 = 2(d+2) 1
- 7. The perimeter of an isosceles triangle is 21 cm. The length of each equal side is triple the length of the base. Find the side lengths of the triangle.
- 8. Solve.

a)
$$\frac{t-6}{2} = 4$$

b) $\frac{1}{3}(c+2) = 1$
c) $\frac{4a+1}{3} = -5$
d) $\frac{2}{3}(s-4) = 4$

9. Solve.

a)
$$\frac{d+4}{2} = \frac{3d}{4}$$

b) $\frac{k-1}{2} = \frac{k+3}{4}$
c) $\frac{2}{3}(q-3) = \frac{1}{4}(q+7)$
d) $\frac{3c-1}{5} = \frac{4c+1}{9}$

- **10.** Rearrange each formula to isolate the variable indicated.
 - **a)** A = lw for l **b)** P = 2a + 2b for b **c)** y = mx for x **d)** l = w + 4 for w**e)** P = 2a + b for b
- **11.** Write an equation for each phrase.
 - a) 4 less than triple a number is 23
 - **b**) the sum of double a number and 6 is 16
 - c) half a number, less 3, is 8
 - **d**) the area decreased by 7 is 14
 - e) the sum of two consecutive integers is 49
 - f) the distance increased by 8 is 25
- 12. Blackie's mass is 4 kg less than Jessie's mass. Together, Blackie and Jessie have a mass of 72 kg. What is each dog's mass?
- 13. Chantal works at a music store. She earns \$8 per hour plus \$0.05 for each CD she sells. Tonight she is working a 5-h shift. How many CDs must Chantal sell to earn \$42?

Unit 3 ANSWERS

1.	a)	7	b)	-4	c)	28	d)	8
2.	a)	-3	b)	-2	c)	3	d)	$\frac{-16}{3}$
3.	a)	11	b)	8	c)	-18	d)	-2
4.	a)	1	b)	3	c)	-2	d)	4
5.	a)	5	b)	2	c)	3	d)	2
6.	a)	-3	b)	4	c)	-1	d)	3
7.	3 c	m, 9 cn	ı, 9	cm				
8.	a)	14	b)	1	c)	-4	d)	10
9.	a)	8	b)	5	c)	9	d)	2
10.	a)	$l = \frac{A}{w}$						
	b)	$b = \frac{P}{m}$	$\frac{-2a}{2}$	<i>1</i>				
	c)	$x = \frac{y}{m}$						
	d)	w = l -	- 4					
	e)	b = P	- 20	a				
11.	a)	3x - 4	= 23	3	b)	2 <i>x</i> + 6 =	= 16	

- c) $\frac{x}{2} 3 = 8$ e) x + x + 1 = 49f) d + 8 = 2512. Blackie: 34 kg; Jessie: 38 kg
- **13.** 40

Unit 4, 5 Review The Straight Line

1.

x	у
0	0
1	0.5
2	1.0
3	1.5
4	2.0
5	2.5

- a) What is the constant of variation for this relationship?
- **b**) Write an equation relating *y* and *x*.
- **2.** Classify each relation as a direct variation, a partial variation, or neither. Explain.
 - **a)** d = 45t **b)** $y = 2x^2 + 3$
 - **c)** y = 2x + 3 **d)** d = 45t + 12
- **3.** Evan earns \$7/h babysitting. The amount he earns, in dollars, varies directly with the time, in hours, he babysits.
 - a) Assign variables. Make a table of values showing Evan's earnings for 0 h, 1 h, 2 h, 3 h, and 4 h.
 - **b**) Describe the graph.
 - c) Identify the constant of variation. What does this represent?
 - **d**) Write an equation in the form y = kx.
- **4.** The relationship between the variables in the table is linear.

x	у
6	61
12	85
14	93

- a) Identify the initial value of *y* and the constant of variation.
- **b**) Write an equation in the form y = mx + b.

- c) Is this partial or direct variation?
- The owner of a small business is having brochures printed. The design cost is \$1500. Printing costs \$0.08 per brochure. The relationship between cost and the number of brochures is a partial variation.
 - a) Identify the fixed cost and the variable cost.
 - **b**) Write an equation for this relationship.
 - c) What is the total cost for 800 brochures?
- 6. Find the slope of each line segment.



- 7. One endpoint of line segment AB is A(3, 4). The slope of this line segment is $\frac{2}{3}$. Find possible coordinates for B.
- **8.** It took 8 min to fill a 52-L bucket.
 - a) What is the rate of change of the volume of water?
 - **b**) Graph the volume of water in the bucket over time.
- **9.** Use first differences. Is each relation linear or non-linear?



10. Tom and Ana ran a race. The graph shows the distance (in metres) each person ran in 10 s.



Who ran faster? How much faster?

11. Find the slope and *y*-intercept of the following line:



12. Identify the slope and *y*-intercept of each line.

a)
$$y = 4x - 5$$

b) $y = -\frac{1}{6}x + 2$

13. Write the equation of a line with each slope and *y*-intercept. Then, graph each line.

a)
$$m = -1, b = 0$$

b) $m = \frac{2}{3}, b = 5$

14. Express each equation in the form y = mx + b.

a) 6x - y = 4

- **b**) x + 4y = 28
- **15.** Identify the slope and *y*-intercept of each equation.
 - **a**) 8x + y = 4
 - **b**) -3x + 2y = 8
- **16.** Identify the *x* and *y*-intercepts of each line. Then, graph the line
 - **a**) 4x 2y = 8
 - **b**) 5x + 3y 15 = 0
- **17.** Which lines are parallel?
 - 2x 3y + 12 = 03y = 2x + 63x - 2y = 03x + 2y = -4
- **18.** Which lines in question 17 are perpendicular?
- **19.** What is the slope of a line that is perpendicular to 3 - x + 4y = 0?
- **20.** Find the equation of a line with a slope of -3, passing through (2, -5).
- **21.** Find the equation of a line parallel to 2x + 5y = 1, with the same y-intercept as x - 4y = 8.
- **22.** Find the equation for a line passing through (3, -4) and (2, 5).
- 23. Ingrid is walking in front of a motion sensor. After 1 s, she is 3.9 m from the sensor. After 3 s, she is 1.7 m from the sensor.
 - a) Find the slope for this relationship.
 - **b**) Write an equation of the form d = mt + b that describes Ingrid's motion.
 - c) After how many seconds will Ingrid's distance from the motion sensor be 0?
- **24.** Solve the following linear system: x + y = 6 and y - 2x = 0.

ANSWERS

1. a)
$$\frac{1}{2}$$
 b) $y = \frac{1}{2}x$

- 2. direct variation a)
 - b) neither
 - partial variation c)
 - d) partial variation.
- 3. a)

Time, t	Earnings, E
0	0
1	7
2	14
3	21
4	28

- **b**) linear, slope of 7, y int of 0
- c) 7; the amount Evan earns each hour he babysits.
- **d**) y = 7x
- **4. a)** 37; 4
 - **b**) y = 4x + 37
 - c) Partial
- **a)** fixed cost: \$1500 5. variable cost: \$0.08 times the number of brochures

b)
$$C = 0.08n + 1500$$
 c) \$1564

6. a)
$$-\frac{2}{5}$$
 b) 5

7. Answers may vary. Possible answer: B(6, 6)8. b)







- **17.** 2x 3y + 12 = 0 and 3y = 2x + 6
- **18.** 2x 3y + 12 = 0 and 3x + 2y = -4; 3y = 2x + 6 and 3x + 2y = -4
- **19.** –4
- **20.** y = -3x + 1

21.
$$y = -\frac{2}{5}x - 2$$

- **22.** y = -9x + 23 **23.** a) -1.1 b) d = -1.1t + 5c) About 4.5 s
- **24.** (2, 4)

Unit 6 Review Measurement

For all questions, round your answer to the nearest tenth of a unit when necessary.

1. Find the length of each indicated side.



2. Find the area of this triangle.



3. Find the perimeter and area of each figure.



4. A pool is 5 m wide by 7 m long. It is surrounded by a deck 2 m wide. What is the area of the deck?



5. Find the surface area and volume of each object.



- 6. Find the side length of each cube.
 - **a**) a cube with volume 3375 cm^3
 - **b**) a cube with surface area 864 cm^2
- 7. Calculate the surface area of each cone.



8. Find the volume of each cone.



- **9.** Find the volume of the largest cone that fits inside a cube with edges 15 cm long.
- **10.** Find the surface area of each sphere.





11. Find the volume of each sphere.



- 12. Which has greater volume?
 - A a hemisphere with radius 12 cm
 - **B** a sphere with radius 8 cm

Answers

- **1.** a) 5.1 cm b) 3.0 cm
- **2.** 7.1 cm^2
- **3.** a) Perimeter: 67.3 cm; Area: 160 cm^2
 - **b)** Perimeter: 21.4 m; Area: 25.4 m^2
- **4.** 64 m^2
- **5.** a) Surface area: 360 cm²; Volume: 400 cm³ **b)** Surface area: 220.5 cm²; Volume: 162 cm³
- **6. a**) 15 cm **b**) 12 cm
- **7.** a) 178.1 cm^2 b) 43.4 cm^2
- **8.** a) 66 cm^3 b) 2513.3 cm^3
- **9.** 883.6 cm^3
- **10.** a) 530.9 cm^2 b) 326.9 cm^2
- **11. a)** 4.2 cm^3 **b)** 33.5 cm^3